

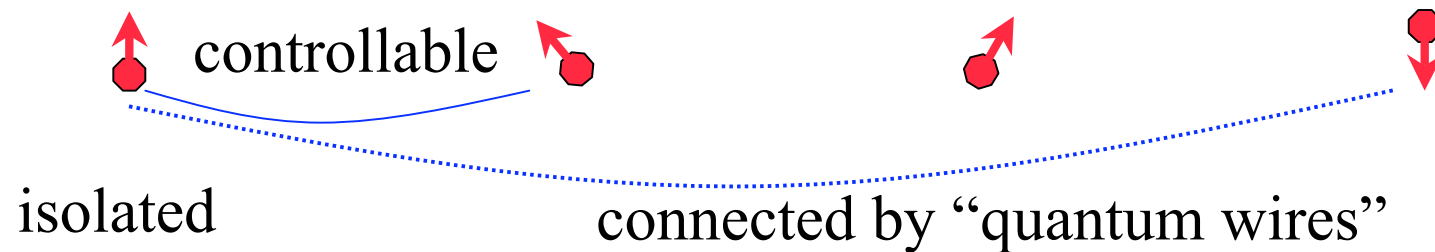
# Controlling individual nuclear spins in diamond: from coherence to scalability

Mikhail Lukin

Physics Department, Harvard University

# Building scalable quantum information systems: an outstanding challenge in science and engineering

## ✓ Quantum bits and quantum wires



## • Solid-state quantum systems

- ✓ Challenge of isolation:  
quantum control in complex solid-state environment

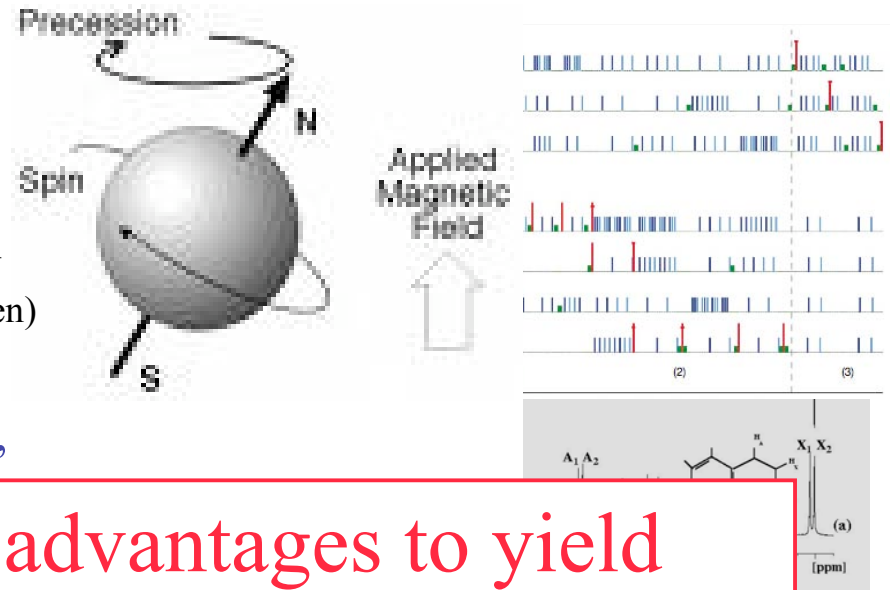
This talk: environment as a resource yields - stable, controllable  
quantum bits

# Spins and photons: best of both worlds

## ✓ Magnetic resonance

Dramatic proof-of-principle NMR quantum computation (e.g. Chuang, Cory, Laflamme, Vandersypen)

- Hard to scale:  
no individual initialization, measurements,



Would like to combine the advantages to yield scalable, robust systems

## ✓ Single photon quantum optics

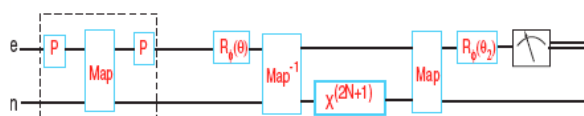
Pure single photon qubits, entangled pairs, ideal for communication, many dramatic demonstrations e.g. teleportation, KLM...

- Hard to scale:  
no memory  
photons do not interact



# Today's talk: novel hybrid approach

## ✓ Electron-nuclear register: key elements

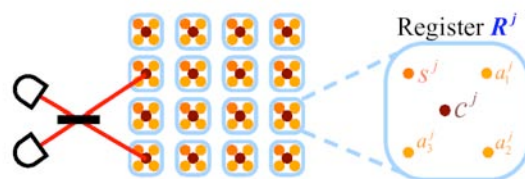


quantum operations with electron and nuclear qubits

coherent coupling of individual nuclei

exceptional isolation: coherence properties of nuclear qubits

## ✓ Scaling up electron-nuclear registers with photons:

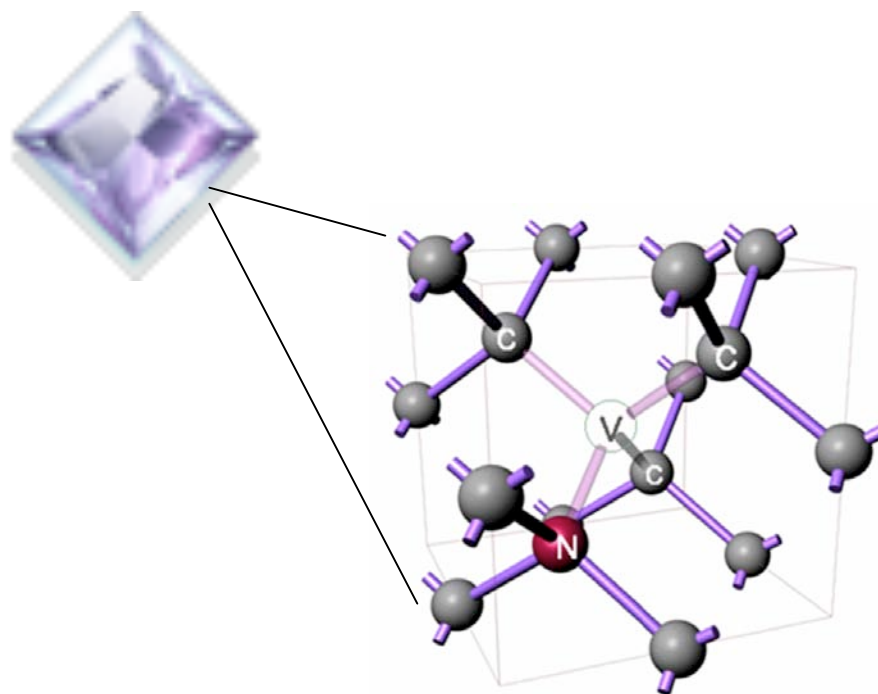


measurement-based optical connects

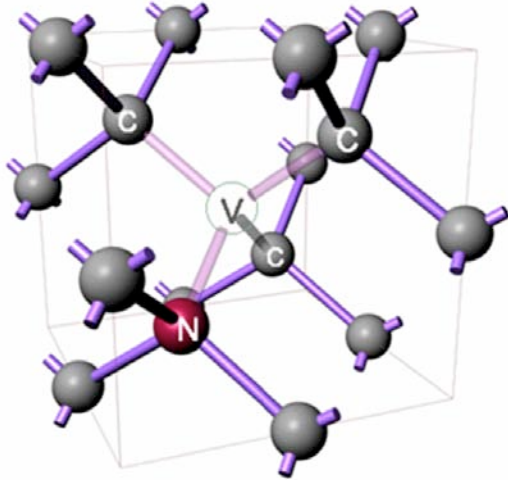
deterministic, measurement-based network approach

## ✓ Outlook

# “Diamond Age”: controlling single electrons and single nuclei



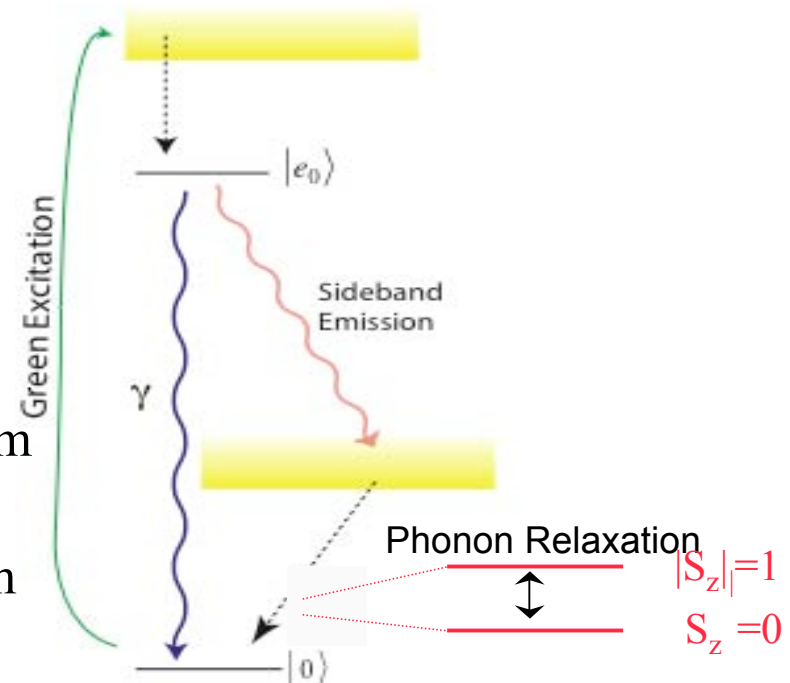
# System: NV color center in high-purity diamond



“Nature’s own trapped molecular ion”  
natural or implanted

## Optical properties

- Sharp zero-phonon emission line @ 637 nm + phonon sidebands 650-730 nm
- Can be excited either by 637 nm or 532 nm

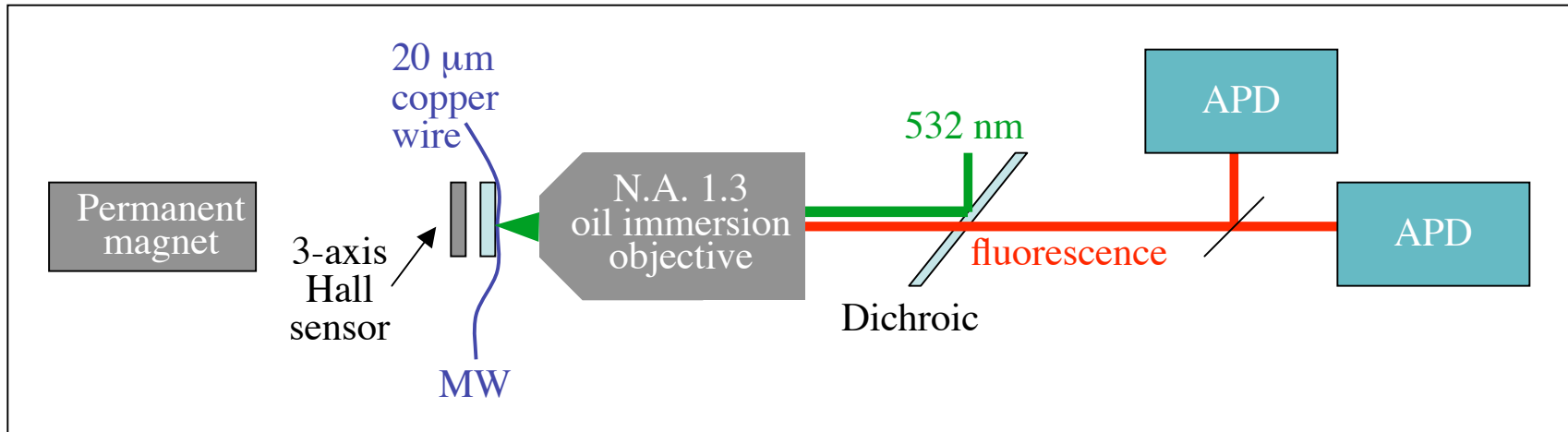


## Ground state properties

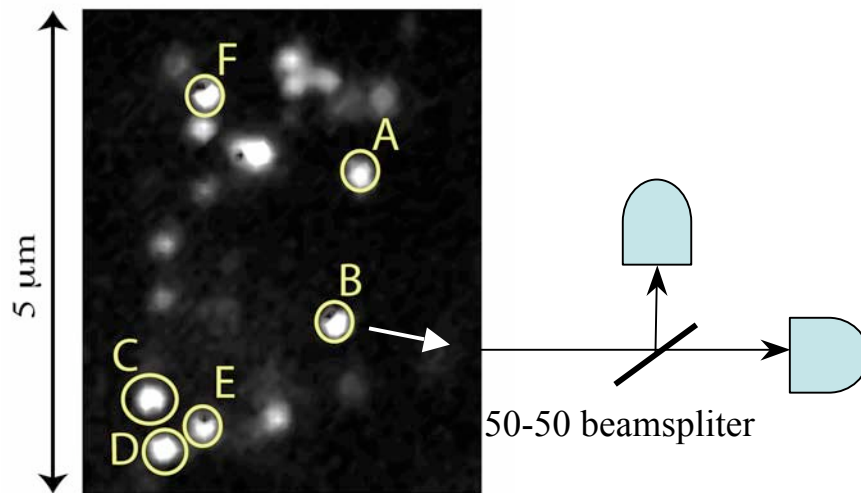
- non-zero electronic spin ( $S=1$ )
- microwave transition:  
zero-field splitting  $\Delta=2.88$  GHz

Early work:  
S.Rand, N.Manson

# Experimental isolation of single centers

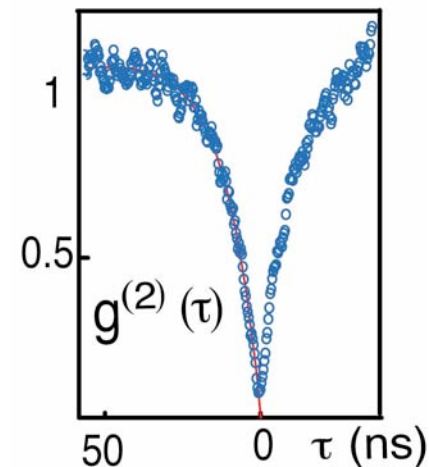


✓ Scanning confocal microscope image



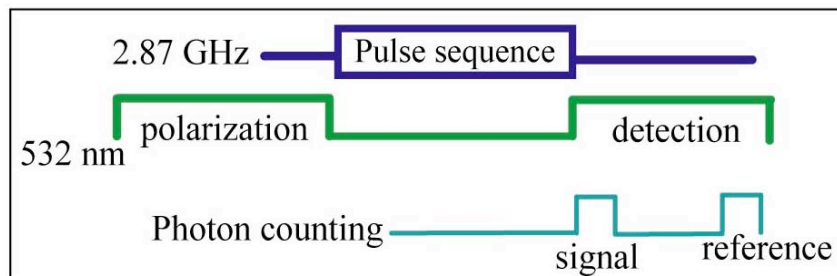
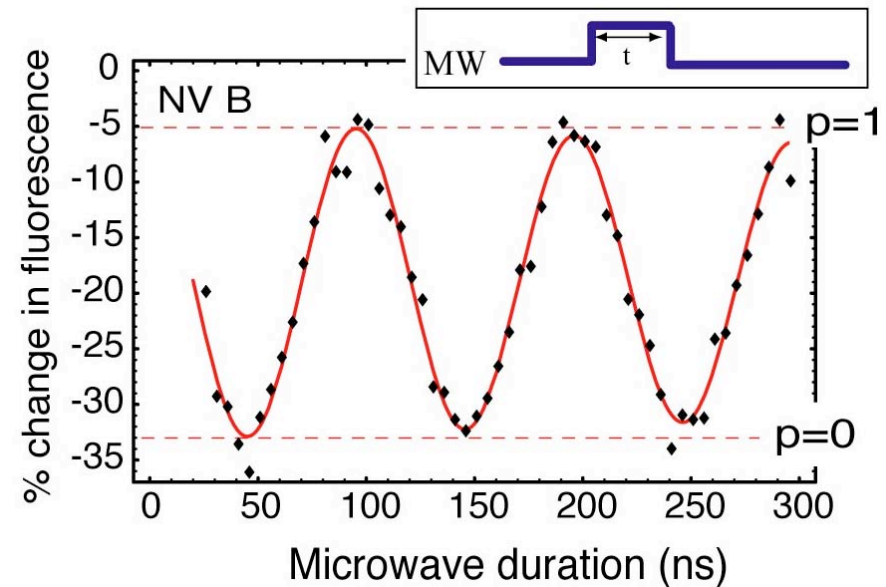
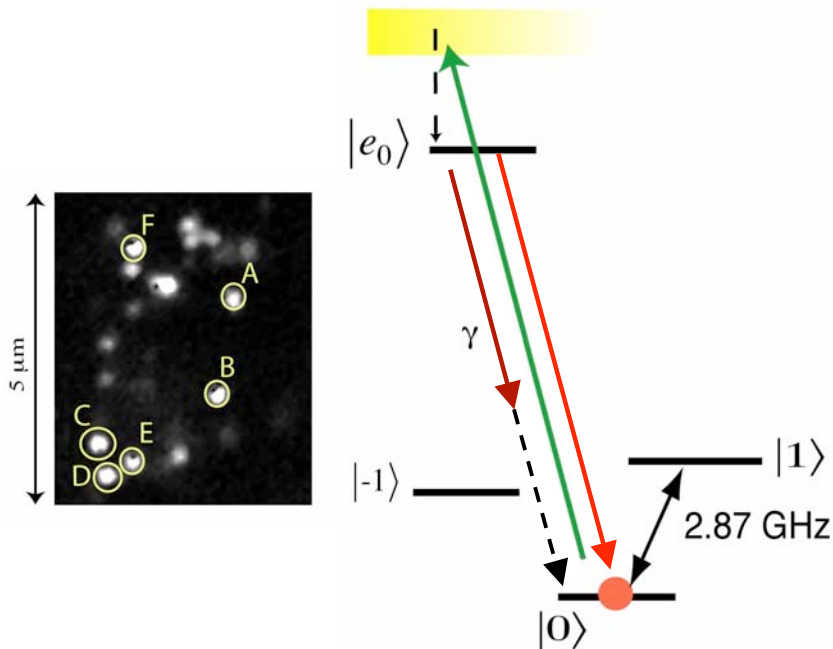
✓ Single photon source:

$\sim 100,000$  cts/sec (Paris, Munich,...)



# Rabi oscillations of single electron spin

Use light to isolate, polarize, readout electron spin state at room T



✓ Pioneering work

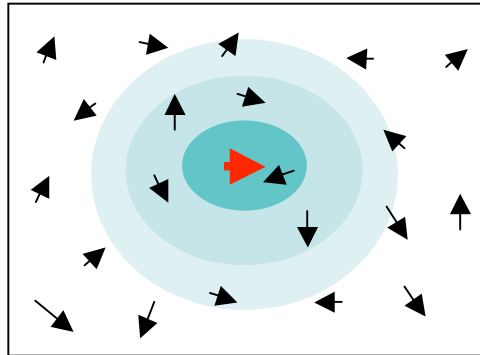
F. Jelezko, J. Wrachtrup (Stuttgart)

Recent work by D. Awschalom (UCSB)

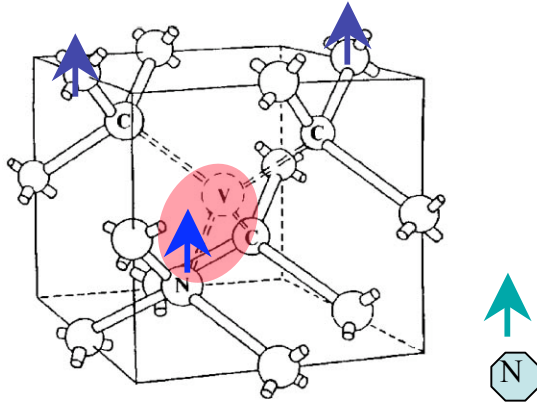
✓ Electron precession decay time (average over many runs):  $T_2^* \sim 1 \mu\text{s}$



# Understanding local environment of single electron spins



# Mesoscopic environment of NV center: sensitive probing via electron spin



- ✓ Stiff, mostly spinless  $^{12}\text{C}$  lattice
  - ✓ Possible contributors:
    - Contact hyperfine interaction:  
single N nuclear spin ( $I=1$ )
    - Coupling to remote spins, e.g.:  
 $\text{C}^{13}$  nuclear spins (few percent)
- Impurity (N) electron spins:  
need pure samples

- ✓ Theory: mesoscopic “spin bath”

$$H = \underbrace{g_0 S_z I_z^N}_{\text{local (N)}} + \sum_j \underbrace{g_j S_z I_n^j}_{\text{non-local}} -$$

“nuclear” field

- ✓ Key observation: nuclear spins are extremely coherent,  
environment can be a very useful resource

# Dynamics of coupled electron and nuclear spins

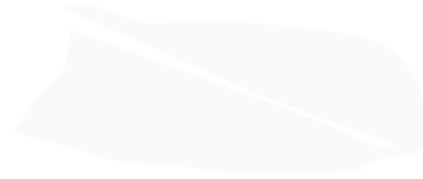
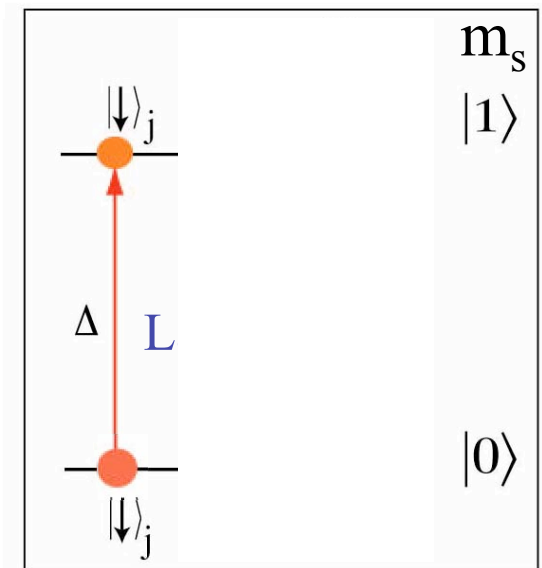
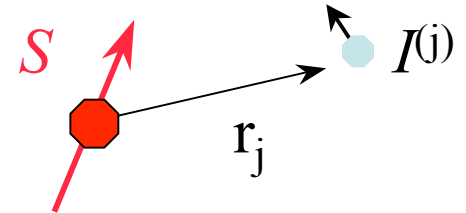
- ✓ Hyperfine interaction of electron with single nuclear spin  $I^{(j)}$

$$V^{(j)} = -\mu_e \mu_n \frac{8\pi |\psi_e(r_j)|^2}{3} \mathbf{S} \cdot \mathbf{I}^{(j)} + \left\langle \frac{\mu_e \mu_n}{r_j^3} \left( \mathbf{S} \cdot \mathbf{I}^{(j)} - 3(\mathbf{n}_j \cdot \mathbf{S})(\mathbf{n}_j \cdot \mathbf{I}^{(j)}) \right) \right\rangle$$

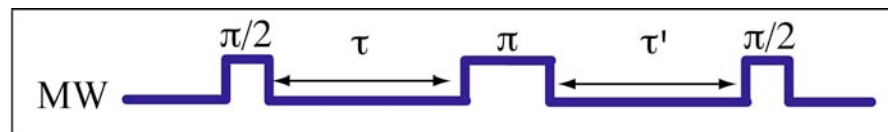
- ✓  $m_s = 1$  electron causes hyperfine splitting of nuclear states
- ✓  $m_s = 0$  electron external field causes Larmor precession

- ✓ Electron-nuclear entanglement dynamics:  
in weak B field electron dynamics is conditional  
upon nuclear state and vice versa

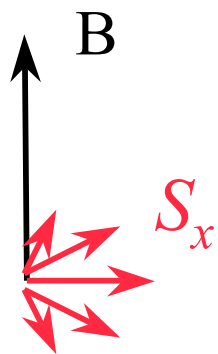
- ✓ Electron spin: sensitive probe of local environment..  
... but typically interacts with a large bath of nuclei  
which results in decoherence



# Probing single electron environment via spin echo

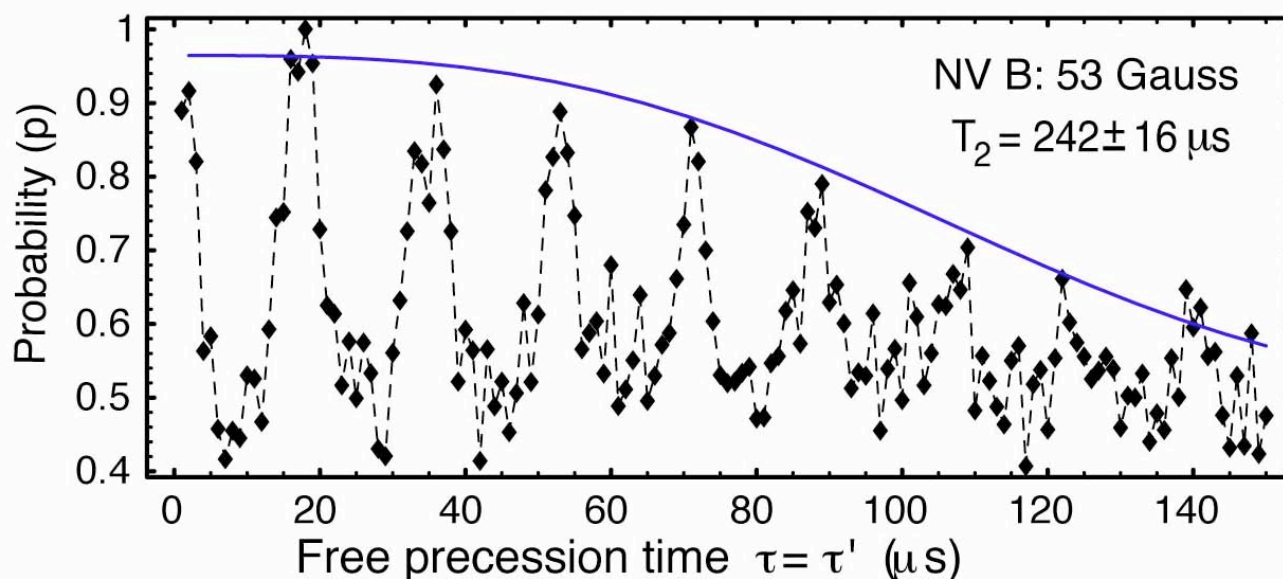


✓ Typical echo we observe



E.Hahn 1950s

*The spin echo signal is only sensitive to changes in the environment which happen faster than  $\tau$*



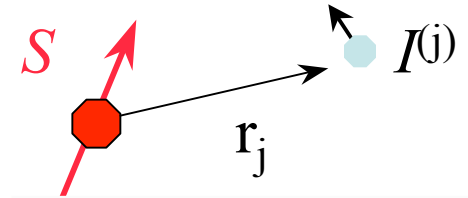
...periodic collapses and revives

- ✓ Big effect:  $T_2 > 200 \mu\text{s} \sim 200 T_2^*$  : environment has long memory
- ✓ Periodic modulation due to Larmor precession of bath  $^{13}\text{C}$  nuclei

Bulk ESR: Electron Spin Echo Envelope Modulation (W.Mims et al, 70s)

# More careful look: proximal nuclei are special

- ✓ Hyperfine interaction of electron with single nuclear spin  $I^{(j)}$



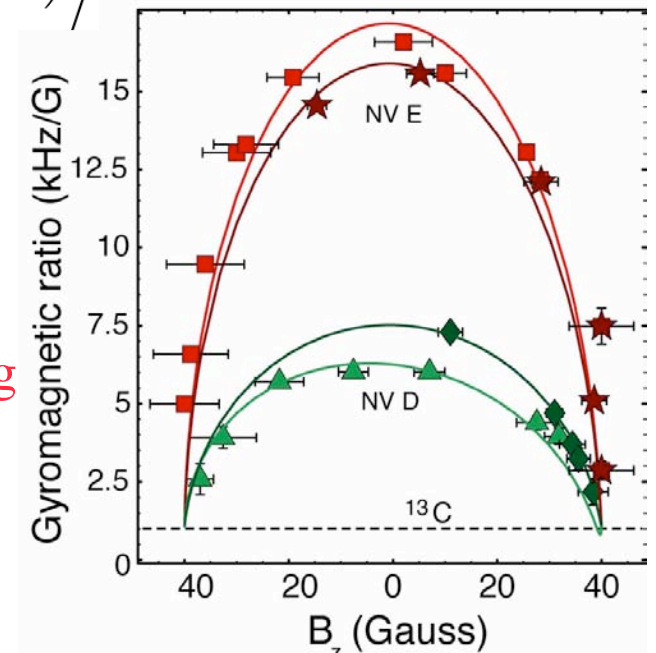
$$V^{(j)} = -\mu_e \mu_n \frac{8\pi |\psi_e(r_j)|^2}{3} \mathbf{S} \cdot \mathbf{I}^{(j)} + \left\langle \frac{\mu_e \mu_n}{r_j^3} \left( \mathbf{S} \cdot \mathbf{I}^{(j)} - 3(\mathbf{n}_j \cdot \mathbf{S})(\mathbf{n}_j \cdot \mathbf{I}^{(j)}) \right) \right\rangle$$

- ✓ Two effects of electron on proximal nuclei due to hyperfine field:

- larger hyperfine interaction
- enhanced Larmor frequency due to hyperfine mixing
- unique “chemical shift”

$$\mu_{\perp}^{eff} \sim \mu_{nuc} + \frac{\langle V(r_j) \rangle}{\Delta} \times \mu_e$$

electron moment  
hyperfine level mixing

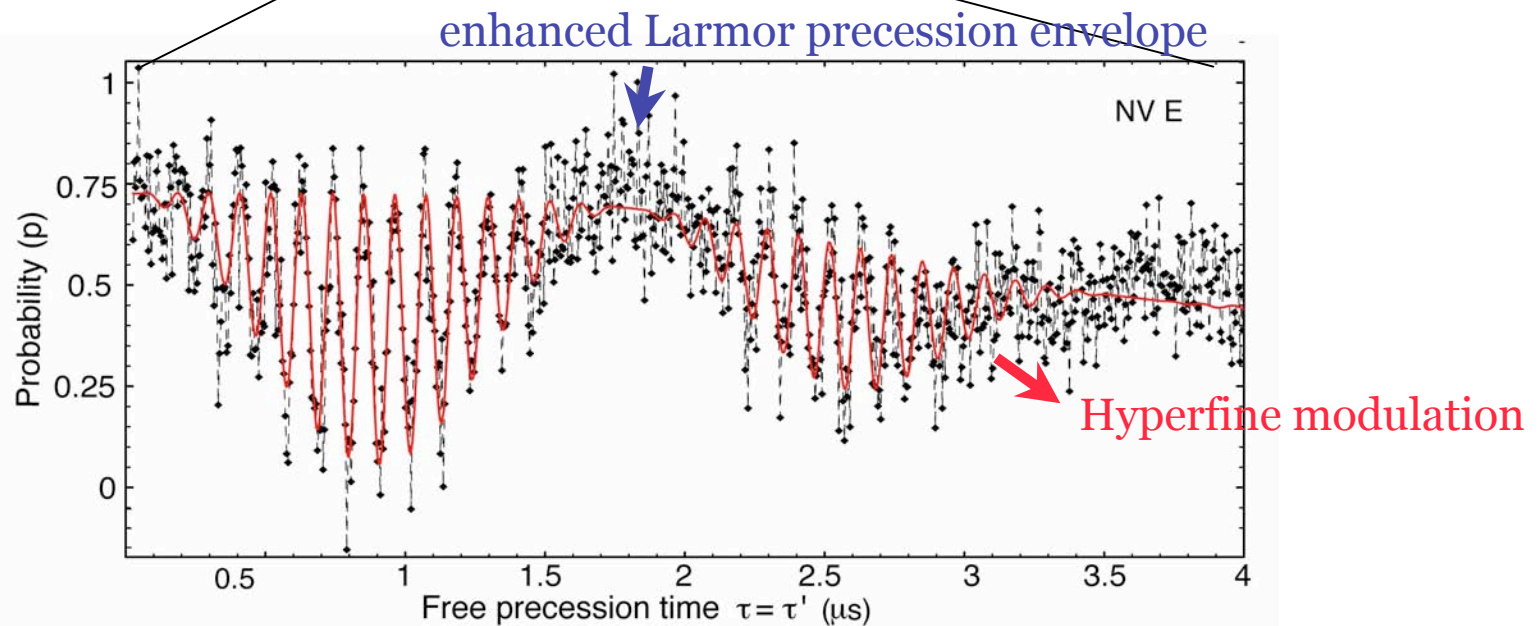
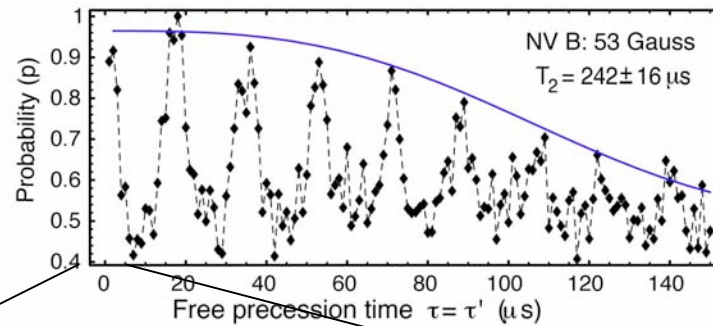
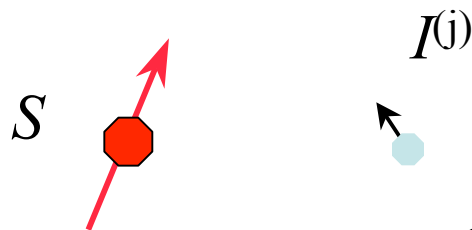


- ✓ Large enhancement since  $\mu_e \sim 10^3 \mu_{nuc}$

Proximal nuclei can be distinguished from the bath!

# Coherent dynamics with individual nuclear spins

- ✓ Electron spin echo at short times

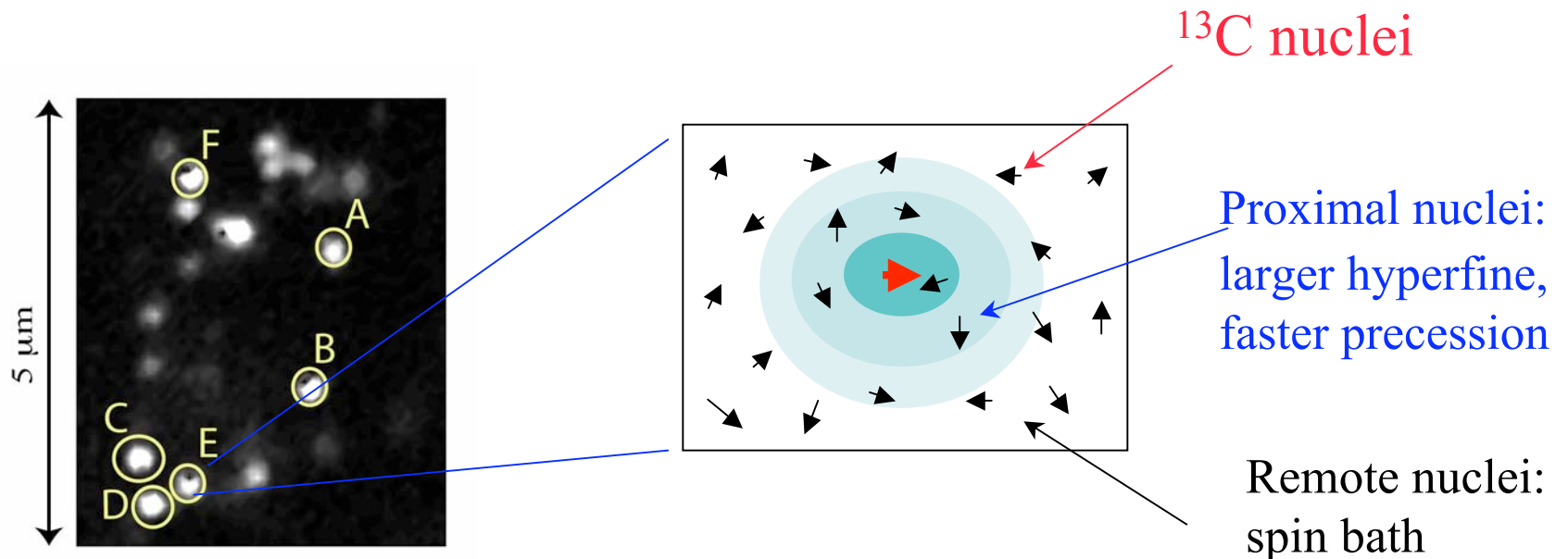


- ✓ Each NV center has its own, specific dynamics, but most display coherent coupling with (some) isolated nuclear spin(s)

L. Childress, M.G.Dutt, J.Taylor, A.Zibrov, F.Jelezko, J.Wrachtrup, P.Hemmer and M.D.L, Science (2006)

# Picture of single electron environment

L.Childress et al, Science (2006)

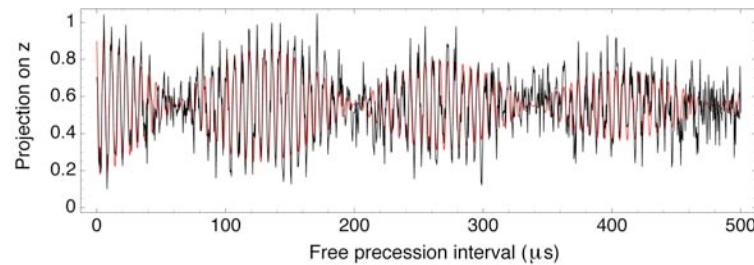


## Environment as a resource

- ✓ Idea: electron spin + few proximal nuclei = controllable quantum system “few qubit register”  
~a kind of large NMR molecule
- ✓ How to polarize, control, read out individual nuclear spins?

Early ideas: Lloyd, Hemmer, Kilin, Wrachtrup, MDL

# Polarizing and measuring individual nuclear spins in diamond lattice

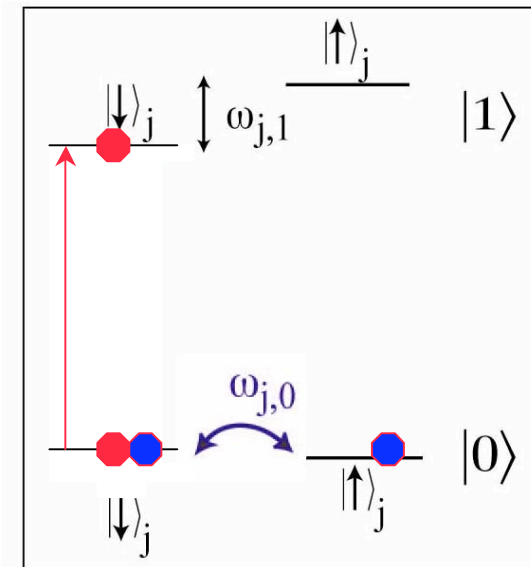
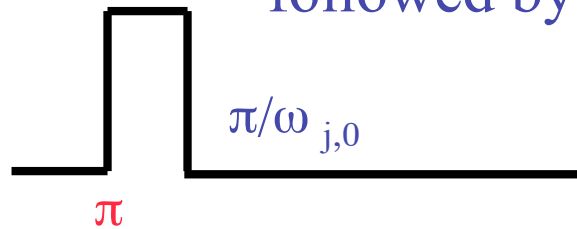




# Manipulating individual nuclear spins: the idea

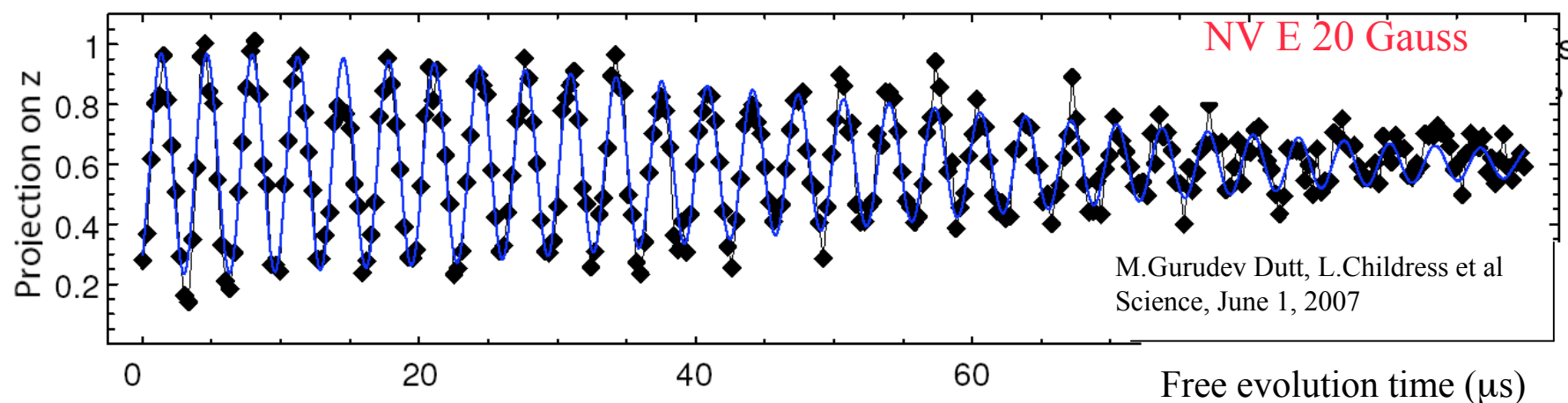
- ✓ Make use of unique hyperfine splitting and chemical shift of proximal nuclei
- ✓ Map qubits between electron to nuclear spin

E.g. selective microwave excitation  
followed by free precession



- ✓ Can be used for
  - preparation (polarization)
  - rotation
  - measurementof individual nuclear spins
- mapping of arbitrary states between electron and nuclei

# Example: watching single nuclear spin precession

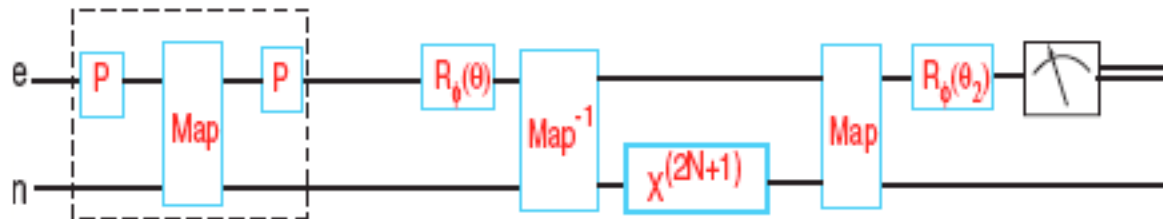


- NMR on single, isolated nuclear spin!

✓ Contrast  $\sim 70\%$   $\Rightarrow$  Nuclear spin preparation  
& readout fidelity  $F \sim 85\%$

This corresponds to effective nuclear temperature  $\sim 300$  nanoKelvin

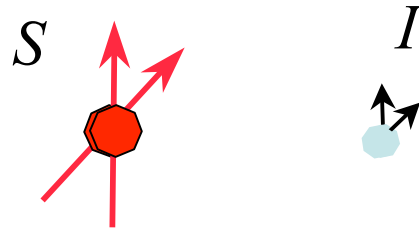
## Quantum register based on single electron and few proximal nuclear spins: key elements



# Quantum control of coupled electron & nuclear qubits

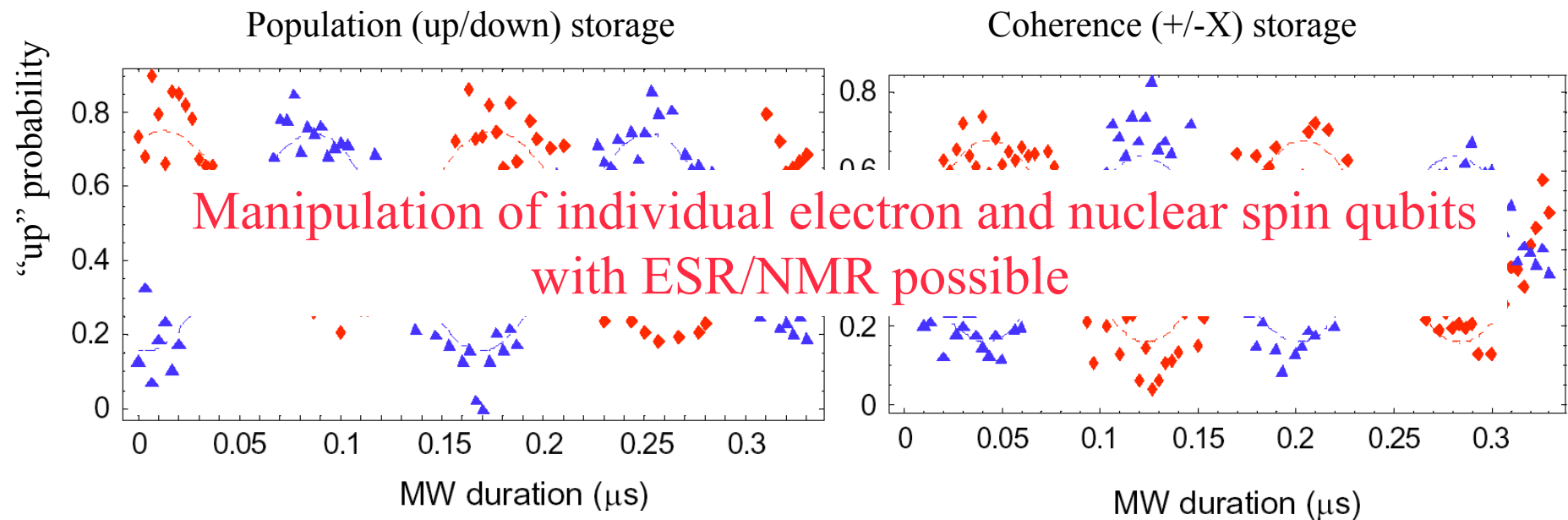
- ✓ Example of quantum operation: storage of arbitrary electron state

MAP



M.Gurudev Dutt, L.Childress et al.  
(2007)

- ✓ Probe: electron Rabi oscillations following storage and retrieval cycle



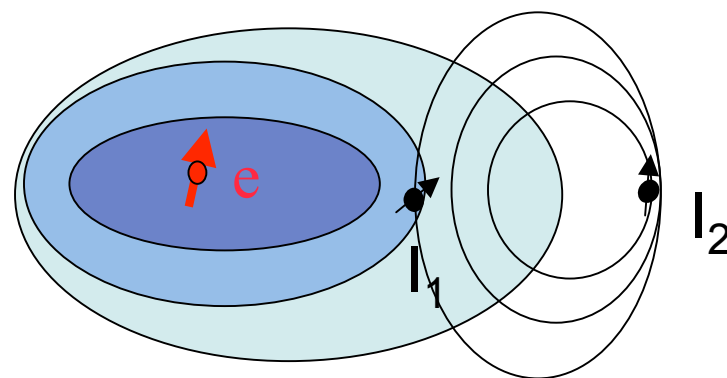
- ✓ Average storage and retrieval fidelity  $F=0.75\pm0.02 > 2/3$

# Coherent coupling between nuclear spin qubits

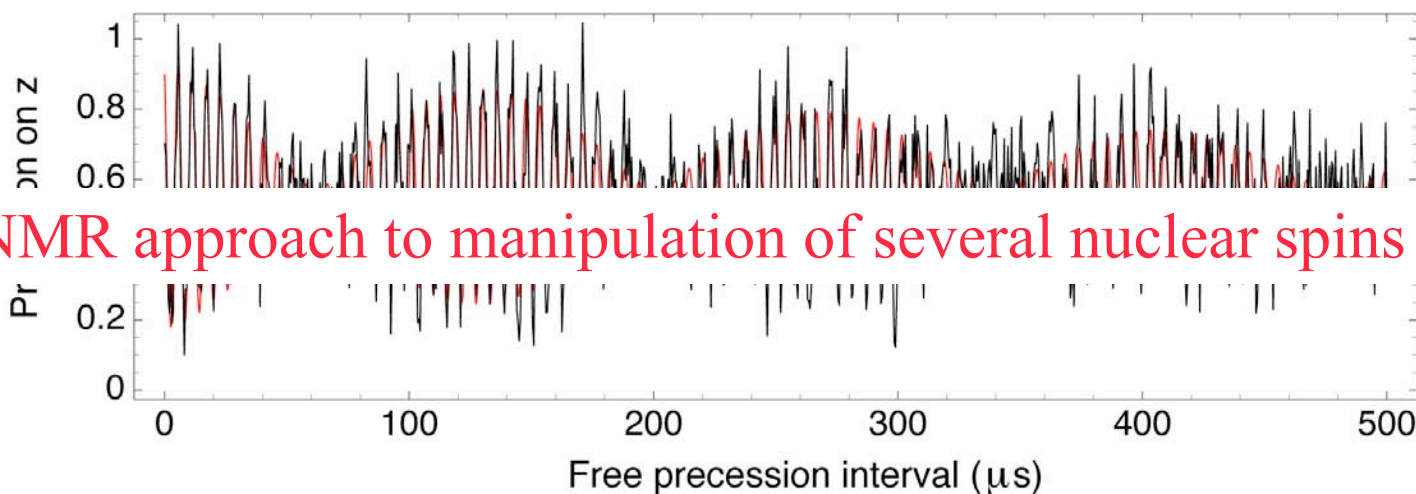
- ✓ Interaction between  $^{13}\text{C}$  nuclear spins

$$H_{12} = \omega_L^1 I_z^{(1)} + \omega_L^2 I_z^{(2)} + \mathbf{I}^{(1)} \cdot \boldsymbol{\beta}^{(12)} \cdot \mathbf{I}^{(2)}$$

- ✓ Zeeman energies different: ZZ interaction
- ✓ Interaction enhanced by proximal electron



- ✓ **Observation:**  $I_1$  nuclear spin precession at long times



**NMR approach to manipulation of several nuclear spins possible**

...modulated due to coherent interaction with another nuclear spin ( $I_2$ ),

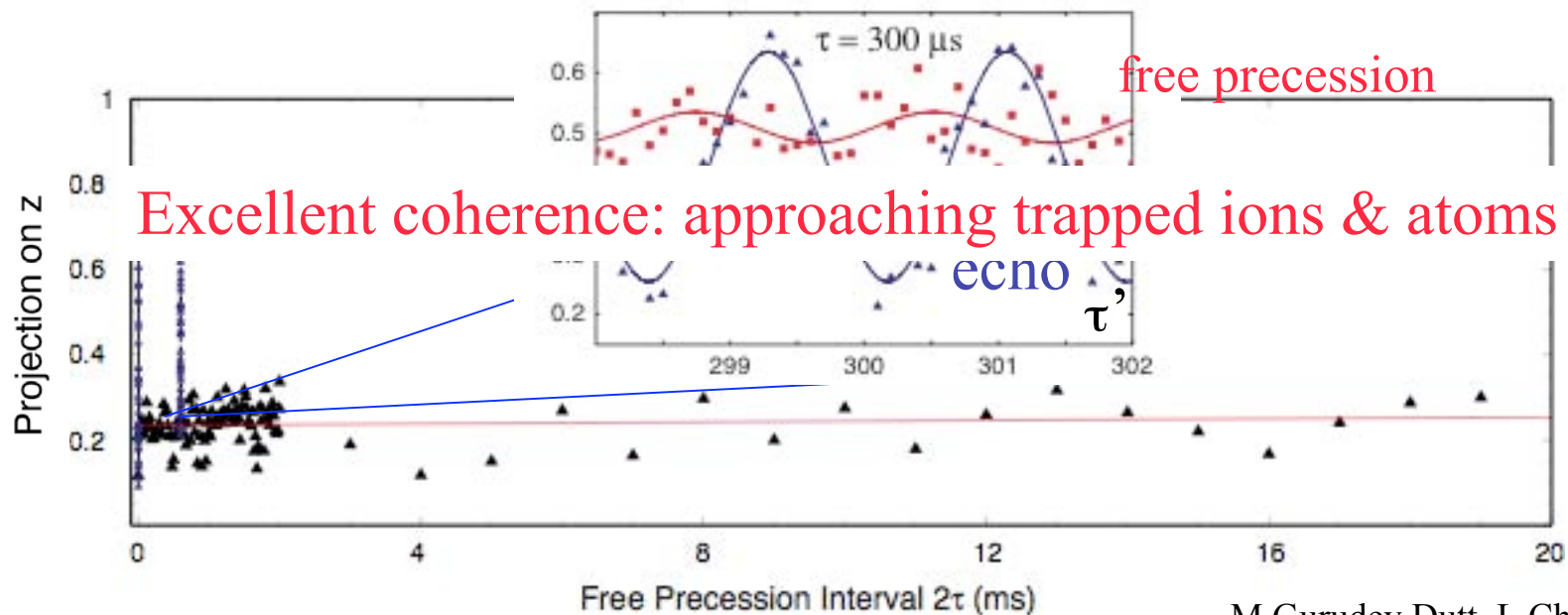
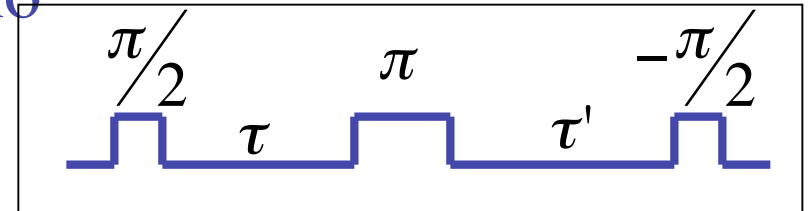
- ✓ Modulation rate controlled e.g. by B field orientation

# Coherence properties of individual nuclear spins

- ✓ Single nuclear spin  $T_2^* = 500 \pm 30 \mu\text{s}$  (longest we've seen)  
Dephasing consistent with being due to (bulk) nuclear spin bath

## Decoupling single nuclei: spin-echo

- ✓ Effective NMR sequence  
(\*with electron's help)



Excellent coherence: approaching trapped ions & atoms

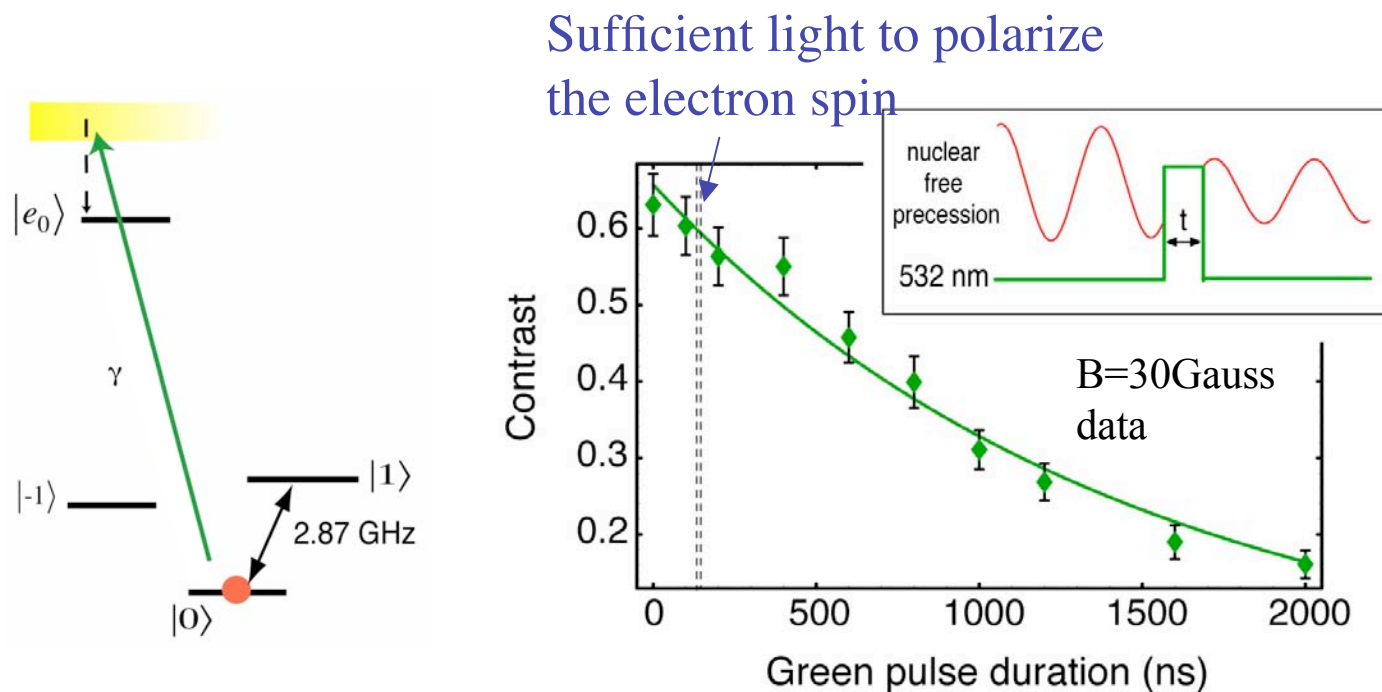
- ✓ Effective decoupling from bulk nuclei:  
 $T_2 \gg 20 \text{ ms}$  ... potentially seconds at room T!

M.Gurudev Dutt, L.Childress et al.  
Science 2007)

# Independent qubit control: isolation of nuclear spins

- ✓ Dipolar couplings can be turned off via NMR-type techniques
- ✓ How well is  $^{13}\text{C}$  isolated during optical excitation of e spin?

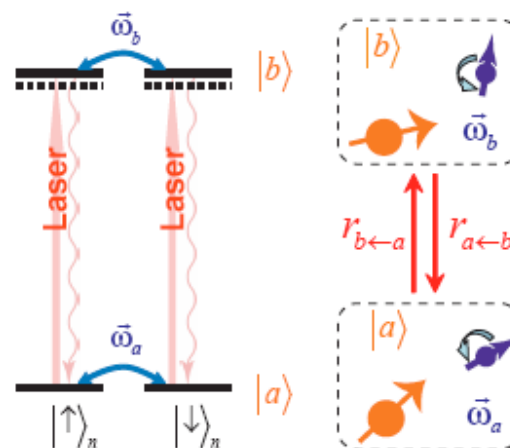
Example: interrogating electron with light during nuclear precession



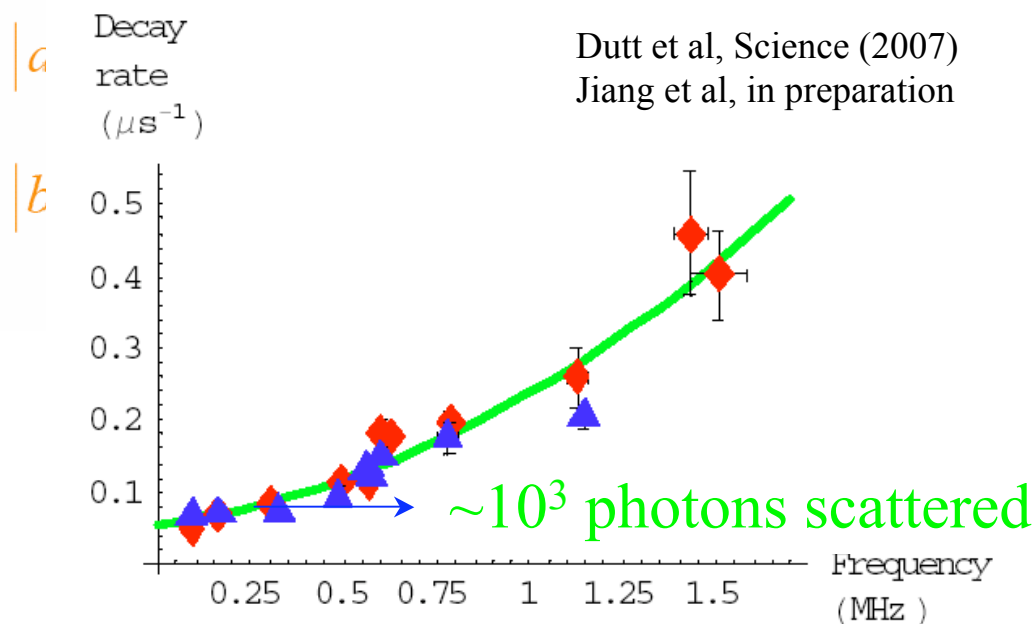
- ✓ Nuclear qubits survive many electron pumping cycles: why?

# Isolating nuclear spin via motional averaging

- ✓ Origin: electron state dependant  
Larmor precession  $\Delta\omega = \omega_a - \omega_b$



- ✓ Physics: random **fast** jumps at rate  $\tau^{-1}$  result in nuclei dephase at  $\Gamma \sim \Delta\omega^2\tau$
- ✓ Result: “motional averaging” of decay for  $\Delta\omega\tau \ll 1$
- ✓  $\Gamma \rightarrow 0$  by reducing B field ( $\Delta\omega \sim B$ )
- ✓ Independent control of electron & nuclear qubits possible
- ✓ Further improvements: e.g. sweet spots, hiding in remote nuclei ...





# Electron-nuclear spin registers: summary

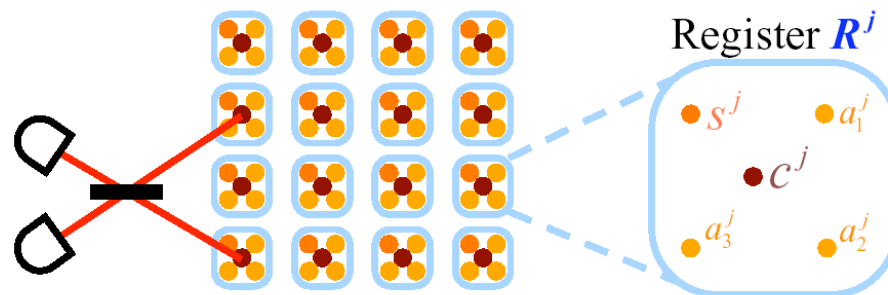
Dutt et al, Science (2007)

## ✓ Key results:

- ✓ Isolated nuclear qubits with excellent coherence properties
- ✓ Few-qubit systems (“registers”) from one electron + several proximal nuclei
- ✓ Robust electron-nuclear and nuclear-nuclear operations via NMR & ESR
- ✓ Isolation of nuclear qubits during optical preparation & readout

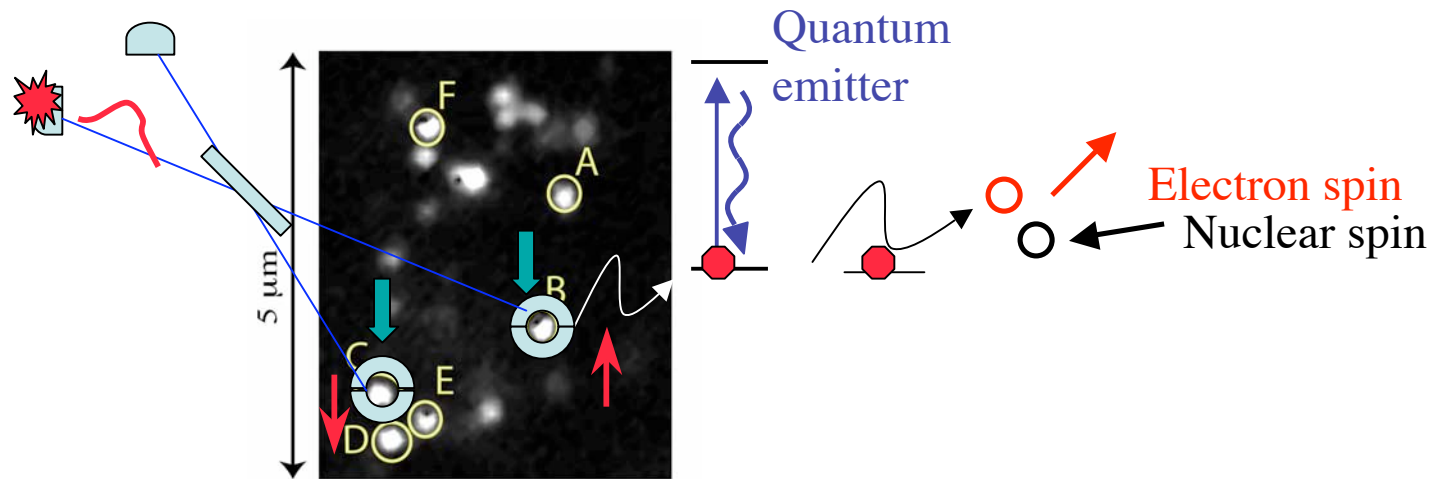
## ✓ Challenge:

coupling between individual, remote, randomly located registers

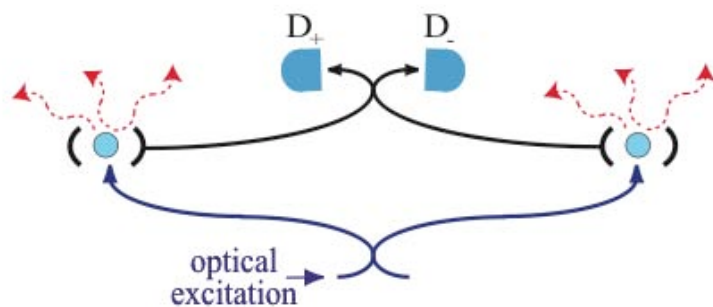


## How to wire them up?

# Linear optical connects for electron-nuclear registers



- ✓ Electron spin entanglement via photon scattering & single photon interference

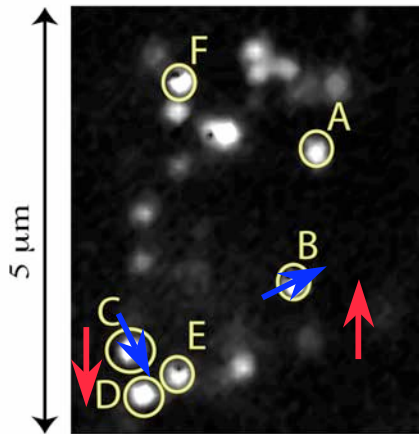


- ✓ Two centers create interferometer: photon detection creates remote electronic singlets!

Example of probabilistic entanglement:

L.Duan, M.Lukin, I. Cirac, P.Zoller Nature 2001, atomic ensembles: experiments Caltech, Gatech, Stanford, Harvard  
I.Cirac and P.Zoller (atoms), L.Duan, C.Monroe (ions), many others

# Useful quantum processors from few coupled qubits



- ✓ Idea: encode qubits in nuclear spins (“storage” qubits)
- ✓ Entangle electrons (“communication” qubits) probabilistically without destroying nuclear qubits
- ✓ Perform deterministic quantum gates between remote nuclei via electron-nuclear coupling: “teleportation based gates”

✓ Operations between any pairs at random locations can be performed simultaneously: purely optical scaling possible

- quantum repeaters for long-distance communication

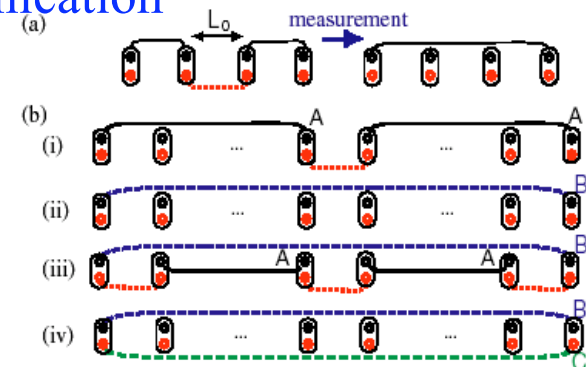
L.Childress, J.Taylor, A.Sorensen. MDL, 2004

- fault tolerant quantum computation

possibly with very high error thresholds

L.Jiang, J.Taylor et al, (quant-ph0703029)

✓ Small registers can be efficiently scaled!



# Progress: efficient entanglement requires narrow optical lines and efficient photon collection

✓ Progress: narrow, stable, tunable optical lines in NV centers

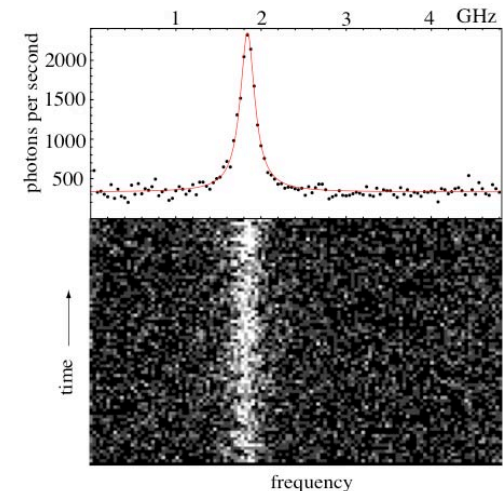
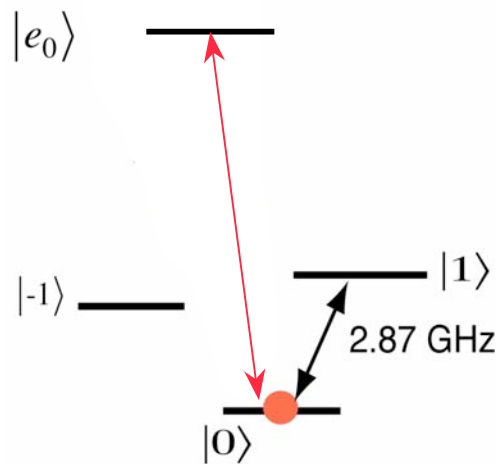
Resonant excitation

@ 637 nm,  $T \sim 10$  K

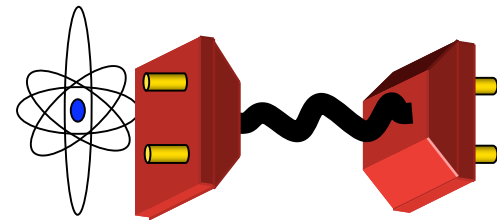
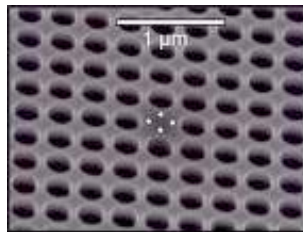
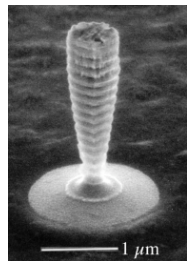
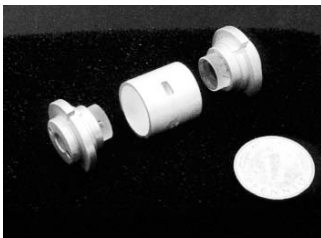
Jelesko et al (Stuttgart),

Santori et al (HP)

Dutt et al (Harvard)



✓ Approaches to efficient photon collection    **New approach:**  
Cavity QED: from Fabry-Perot to photonic crystals    **nanowire surface plasmons**



Kimble, Rempe, Yamamoto, Vuckovic, Imamoglu, Loncar ...

Chang et al, PRL (2006) theory  
Akimov et al, (2007) experiment

# Outlook

New systems: e.g. other nano-tubes,  
other carbon-based materials

New applications:  
e.g. ultra-sensitive, high resolution  
magnetometer  
based on NV electron spins

New interface of NMR, mesoscopics, quantum optics,  
photonics, materials technology and quantum information

NMR manipulation of  
multi-qubit register  
with high polarization and  
single spins addressing

Entanglement of remote  
nuclear  
spins in solid-state

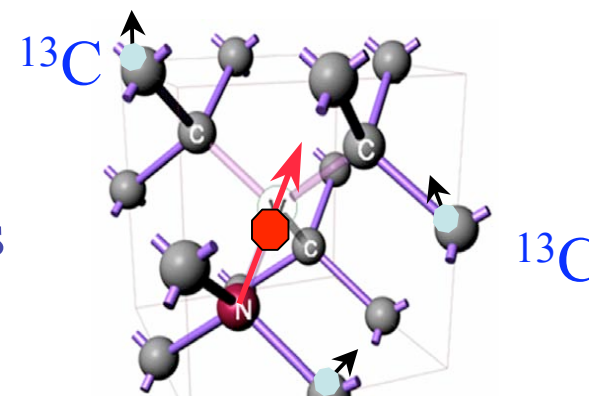
Systems for efficient  
photon collection:  
photonic crystals,  
plasmons...

Quantum repeaters and novel  
approaches to FTQC,  
e.g. measurement-based,  
cluster-state...

# Summary

## ✓ Understanding (nuclear spin) environment of single electrons

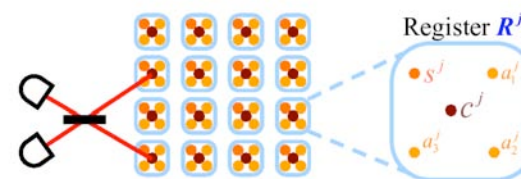
- Addressing individual nuclear spins in diamond lattice



- Coherent coupling between nuclear spin qubits

## ✓ Hybrid approaches to scalable QI systems

- Measurement-based optical scaling of electron-nuclear spins registers
- New approaches to scalable system architecture



## Harvard Quantum Optics group

Gurudev Dutt	Jake Taylor --> MIT
Lily Childress	Axel Andre --> Yale
Darrick Chang	Michal Bajsci
Aryesh Mukherjee	Anders Sorensen --> Niels Bohr Inst
Liang Jiang	Ehud Altman --> Wiezmann
Alexei Gorshkov	Dmitry Petrov --> CNRS
Vlatko Balic	Matt Eisaman --> NIST
Philip Walther	Anatoly Polkovnikov --> BU
Alexey Akimov	Alexander Zibrov
Jeromino Maze	Ana Maria Ray

### Collaboration with

[Phil Hemmer](#) (Texas A&M), [Fedor Jelezko](#), Jeorg Wrachtrup (Stuttgart)  
Eugene Demler (Harvard) & Jelena Vuckovic, Yoshi Yamamoto (Stanford)  
[Hongkun Park](#) (Harvard-Chemistry)

\$\$\$ NSF, Packard Foundations

quantum registers: [ARO-MURI](#), [NSF-PIF](#)  
plasmon QED: [NSF-NIRT](#), [DARPA](#)